



## **Designing a Mechanism for Reallocation of Spectrum with Incentive-based Pricing**

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Joint Research Project  
Spectrum Valuation for 3G Services:  
Application of the 1900 MHz Band

10 – 14 November, 2008, Bangkok

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**Designing a Mechanism for Reallocation of Spectrum  
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## **I. INTRODUCTION**



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## I. A. Objective of this paper

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incentive-based pricing (IBP)  
of spectrum



## I. B. Spectrum use in the future (1/3)

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Power of mobile communication:

in the past, direct meeting only

now mobile-connected in voice

*broadband connection* in the future

informational ‘teleportation’



## I. B. Spectrum use in the future (2/3)

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What do we need to bring in broadband?

(1) more spectrum

*spectrum reallocation* is important  
to promote technological progress and  
new business initiative



## I. B. Spectrum use in the future (3/3)

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What do we need to bring in broadband?

(2) use of economic incentives

some *economic mechanism* for  
converting private efforts into a  
public goal



## I. B. Spectrum use in the future (3a/3)

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Goal:

To let spectrum be used by those who can best promote the benefits of the people



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## II. SPECTRUM AS AN ECONOMIC RESOURCE --- A SHORT OVERVIEW



## II. A. What is spectrum? (2/2)

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- spectrum is a **real estate**,  
like land, producing “**rent**”  
(income to nonsubstitutable factor  
of production)
- management of spectrum rents



## II. A. What is spectrum? (2a/2)

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- history of spectrum use:  
started 100yrs ago with tech regulations  
no scarcity (no rent) until 1990's  
has become scarce with mobile tech  
huge rents & vested rights



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### **III. VALUE OF SPECTRUM BLOCKS TO USERS**



### **III. A. Theory of valuation (in general) (1/13)**

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#### **1. value of economic objects in competitive-market environment**

economic objects:

- property, e.g. , land, houses
- organization (e.g., a corporation)
- human labor
- spectrum blocks



### III. A. Theory of valuations (in general) (7/13)

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supply value (**supply price**):

when the owner is about to yield  
the ownership of the object.

demand value (**demand price**):

when a (potential) owner is about  
to acquire the object.



### III. B. Spectrum valuation by incumbent users: (1/12)

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#### 1. formula:

$p_1$  : the value of (incumbent) user with  
a spectrum block

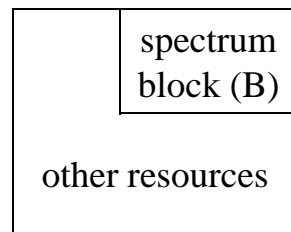
$p_2$  : the value of the user without  
the block

The value of the block to the user:

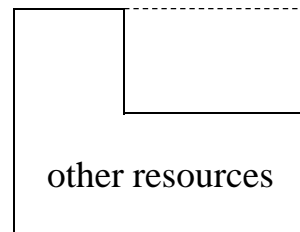
$$P_X^* = p_1 - p_2$$



**Figure IIIB.1: Business resources of X  
with and without the block B**

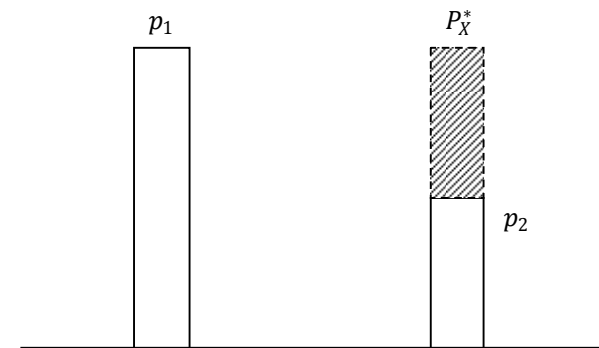


**A:** With the block



**B:** Without the block

**Figure IIIB.2: Value of X with and without B and  
the supply price of B by X**



**A:** With the block

**B:** Without the block



### III. C. Spectrum valuation by potential users (1/13)

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#### 1. formula:

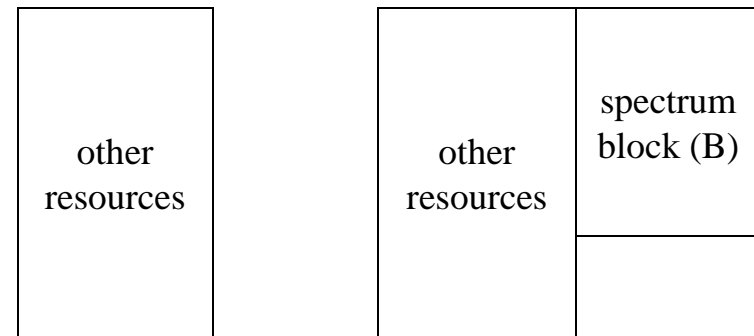
$q_1$  : the value of (potential) user without  
a spectrum block

$q_2$  : the value of the user with the block  
the value of B to the user:

$$P_Y^* = q_2 - q_1$$



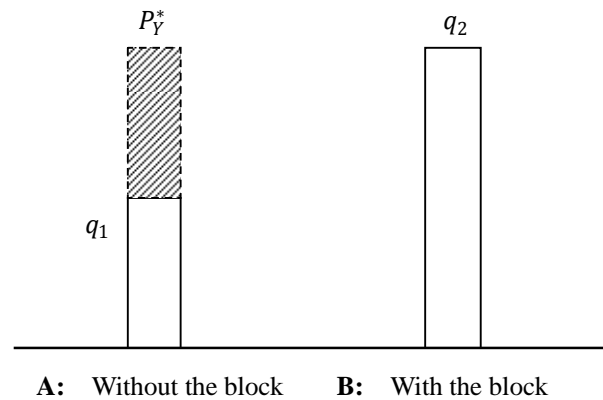
**Figure IIIC.1: Business resources of Y  
without and with the block B**



**A:** Without the block

**B:** With the block

**Figure IIIC.2: Value of Y without and with B  
and the demand price for B by Y**



### III. D. Welfare and trade implications of spectrum valuation (1/7)

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#### 1. assumptions:

spectrum block B

$P_X^*$ : the supply price of B to  
incumbent user X.

$P_Y^*$ : the demand price for B to  
potential user Y.

### III. D. Welfare and trade implications of spectrum valuation (2/7)

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#### 2. welfare implications:

- a. If  $P_Y^* > P_X^*$ , then the sum of the value of X and that of Y combined will be increased by  $(P_Y^* - P_X^*)$  if B is transferred from X to Y.



### III. D. Welfare and trade implications of spectrum valuation (3/7)

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In short, welfare improvement is achieved by a transfer of B from X to Y both at the individual and the aggregate levels

(Pareto improvement =  
increased efficiency of spectrum use)



### III. D. Welfare and trade implications of spectrum valuation (4/7)

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In reality, however, most of the spectrum blocks are being used inefficiently in the Pareto sense.

Reason (historical): Continuation of the old-time use of spectrum, formed when spectrum was not scarce.



### III. D. Welfare and trade implications of spectrum valuation (5/7)

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(increase in income by transfer of B: from Y to X )

$$= P_Y^* - P_X^*$$

(measure of efficiency improvement)

$$= 1.0 - \left( \frac{P_X^*}{P_Y^*} \right)$$

(measure of aggregate efficiency improvement)

$$= 1.0 - \frac{\sum P_X^*}{\sum P_Y^*}$$



### III. D. Welfare and trade implications of spectrum valuation (6/7)

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#### 3. trade implications:

- a. If  $P_Y^* > P_X^*$ , and if X and Y can agree upon a price  $p$  such that  $P_Y^* \geq p \geq P_X^*$  for trading B from X to Y, then trade of B will take place.



### III. D. Welfare and trade implications of spectrum valuation (7/7)

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- b. If  $P_Y^* > P_X^*$ , but X and Y cannot agree at a price  $p$  such that  $P_Y^* \geq p \geq P_X^*$ , then trade of B may not take place in spite of the possibility of welfare improvement to one or both of X and Y by trading B.



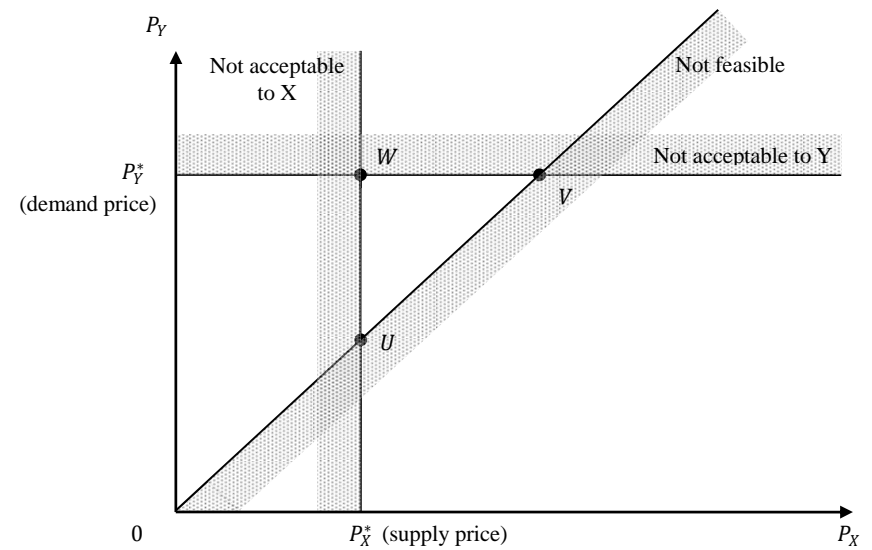
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## IV. TRADE OF SPECTRUM BLOCKS BY DIRECT BARGAINING



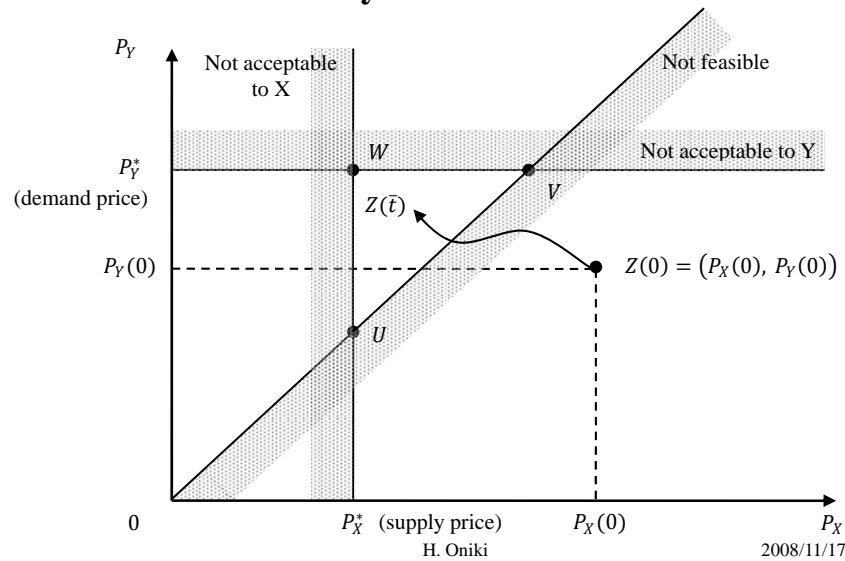
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**Figure IVB.1: Trade prices of block B**



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**Figure IVD.1: Example of bargaining  
by X and Y of block B**



## IV. E. Business conditions of incumbent and potential users (1/4)

### 1. incumbent user (X):

running business using B

with **extra profits incl rent on B**

business condition is good with  
accumulated profits

no urgent need to sell B



#### IV. E. Business conditions of incumbent and potential users (2/4)

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##### 2. new user (Y):

creating new business on starting  
new use of B  
no extra profits accumulated  
need to pay interests/dividends  
on newly prepared capital  
urgent need to obtain B



#### IV. E. Business conditions of incumbent and potential users (3/4)

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##### 3. effects on bargaining:

a. maximum trade periods:

Y cannot wait for long as X can





#### **IV. E. Business conditions of incumbent and potential users (4/4)**

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b. the rate of revising prices offered/bid:

Y revises prices faster than X does.

c. likely outcome: no trade(!!)



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## **VI. CONVENTIONAL MARKET MECHANISM FOR SPECTRUM TRADE**



## VI. A. Assumptions:

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1. market is decentralized.
2. incumbent and potential users meet randomly in the market to form a pair of an incumbent user and a potential user.



## VI. B. Expected outcome:

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Pareto-improving trade will be achieved but only to a limited extent. The overall economic state will remain suboptimal after the market is closed.



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## VII. EXTENDED MARKET MECHANISM (EMM) FOR SPECTRUM TRADE



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### VII. A. Outline (1/2)

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1. market is centralized and operated  
by government



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## VII. A. Outline (2/2)

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2. incumbent users are asked to reveal their supply prices (false revelation is possible) and to pay spectrum holding fees



## VII. B. Bill of spectrum rights and responsibilities (proposed) (1/4)

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1. Spectrum is a property owned by the people collectively; the benefits of using, and the income from operating, spectrum shall therefore be attributed to the people.



## VII. B. Bill of spectrum rights and responsibilities (proposed) (2/4)

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2. Spectrum may be used exclusively by a user for an **indefinite period**; the right to use spectrum, however, is by no means permanent.



## VII. B. Bill of spectrum rights and responsibilities (proposed) (3/4)

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3. The user shall yield the right of using spectrum when requested by a party with a compensation which exceeds the amount declared by the user prior to such a request.



## VII. B. Bill of spectrum rights and responsibilities (proposed) (4/4)

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4. The user shall pay each year to the government a usage fee, which is equal to the product of the declared compensation and a fee rate to be specified by the government.



## VII. C. Rights and obligations of incumbents

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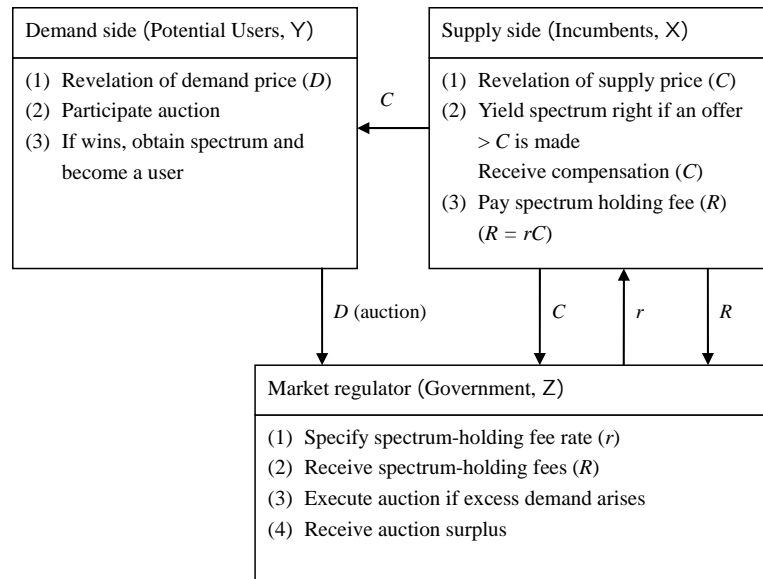
tradeoff to incumbents

“holding up” a block or a group  
may be costly



**Figure VIIA.2: Organization of EMM**

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## VII. E. Roles of government with EMM:

### 1. spectrum holding fee

a. determines a fee rate ( $r$ ):

to control the speed of reallocation  
resembles to determination of  
discount rate by central bank

b. receives spectrum fees ( $R$ )



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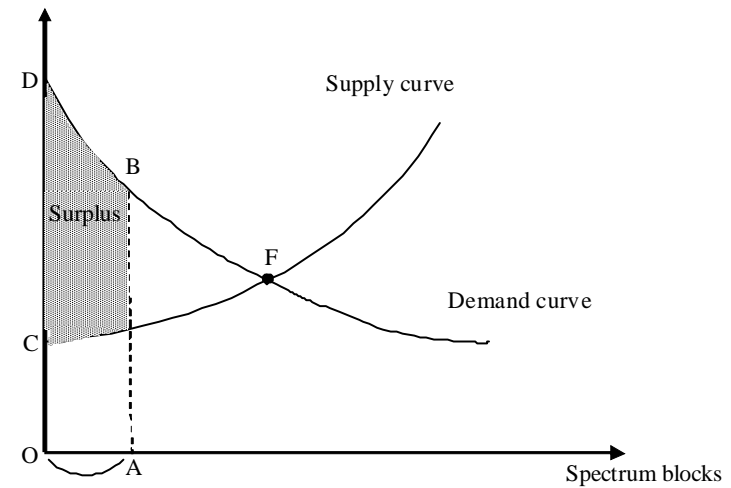
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## VII. F. Expected outcome from EMM:

Pareto-improving reallocations will be realized gradually step by step  
 speed of reallocation is controlled  
 by  $r$



**Figure VIII F3: Spectrum trade expressed by means of “Demand and Supply” Curves**





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## VIII. APPLICATIONS AND EXTENSIONS OF EMM



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### VIII. A. Secondary (indirect) users of spectrum with EMM (1/2)

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#### 1. Commons users:

primary user:

commons administrator

secondary users:

general users (the public)

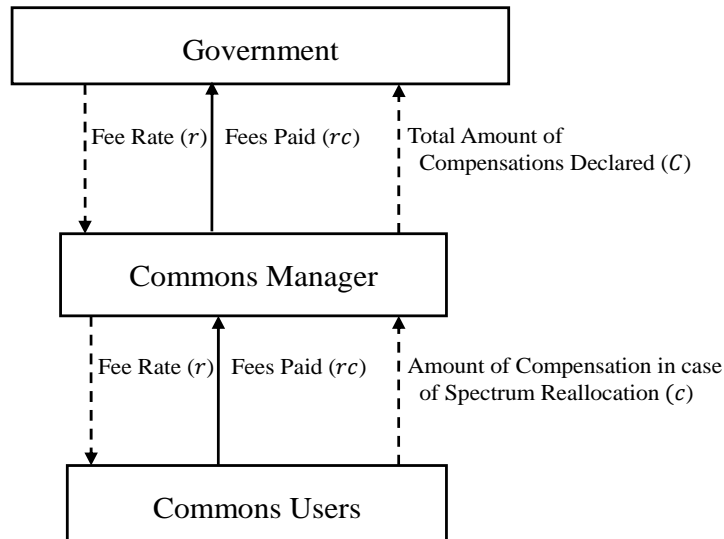


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**Figure VIIIA.1: Supply Price Revealed by Common Users**

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**VIII. A. Secondary (indirect) users of spectrum with EMM (2/2)**

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**2. Subscribers to service using spectrum:**

ex.: mobile phone users

wireless internet users

primary user: providers, broadcasters

secondary users: subscribers, “users”

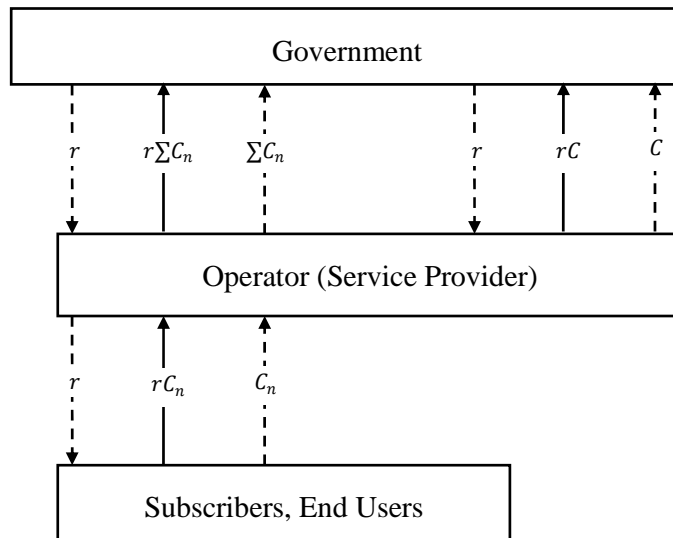


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**Figure VIIIA.2: Supply Price Revealed  
by a Service Provider and Subscribers**

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## VIII. B. Introduction of reallocation as a forward trading, forward supply price

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EMM with timing of reallocation specified

ex.: reallocation  $x$  years after the current year

$x = 1, 3, 5$  and  $10$  years

$c, C, D, r$  to be specified for each  $x$ .

EMM is applied for each  $x$ .

actual reallocation to be done in the year  $x$ .

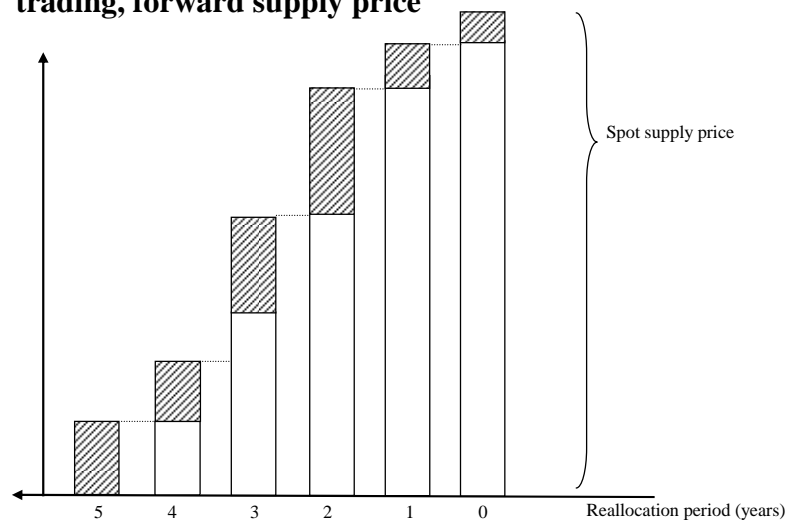


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**Figure VIII.B. 1: Introduction of reallocation as a forward trading, forward supply price**

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Note : A shaded area denotes the increase in the supply price when the period of trade execution is shortened by 1 year.

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## VIII. C. Preventing speculation with EMM

speculation is possible on a strategically positioned block wrt externalities

regulation:

impose a penalty on a steep increase in  $C$ .

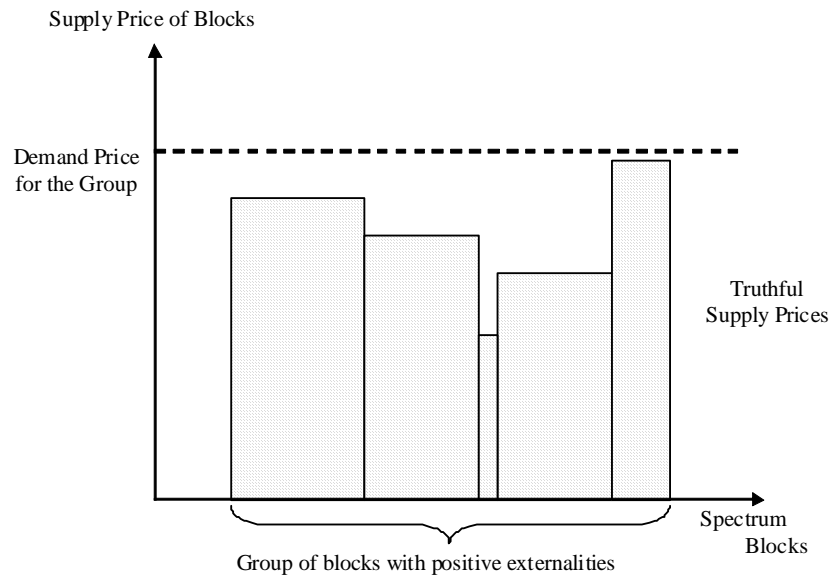


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**Figure VIII.C. 1: Example of truthful supply prices**

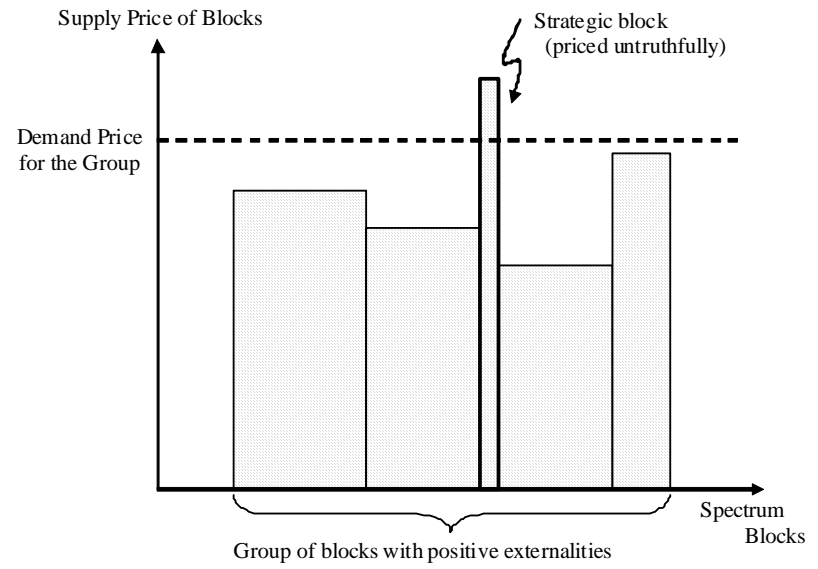
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**Figure VIII.C. 2: Examples of truthful and untruthful supply prices**

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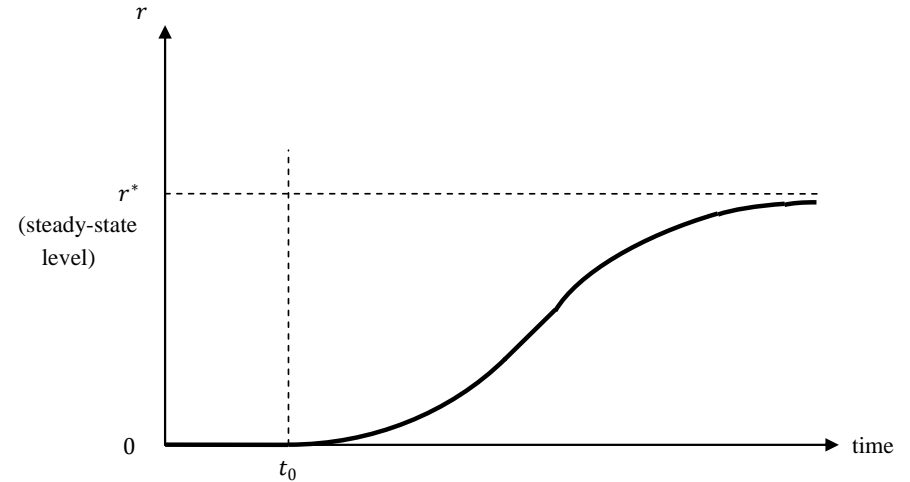
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### VIII. D. Transition from the current system to EMM

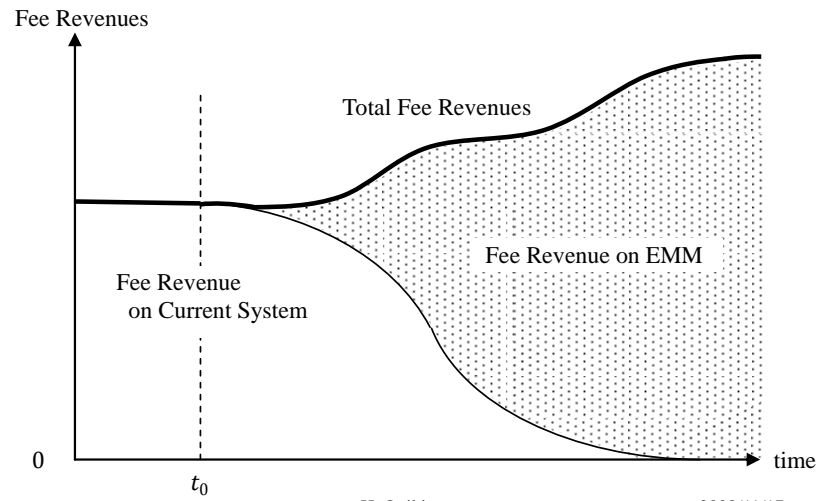
gradual transition is recommended  
 no “big bang”  
 set  $r$  at a level close to zero initially  
 increase  $r$  gradually thereafter  
 decrease the rate for current spectrum fees  
 simultaneously



Figure VIII.D.1:  
 Proposed time path of spectrum-fee rate



**Figure VIIID. 2:**  
**Expected change of spectrum-fee revenues**



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